A rapid and accurate computer vision system for measuring the volume of axi-symmetric natural products based on cubic spline interpolation

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ABSTRACT

The volume contains prominent information used to evaluate the visual quality of natural products and can be measured using a computer vision system. The computer vision system provides an alternative method for measuring the volume of natural products, especially for axi-symmetric natural products. The volume of axi-symmetric natural products can be obtained using integral for the volume of solid of revolution by rotating the boundary curve of the upper half object cross-section. This study proposes a computer vision system for measuring the volume of axi-symmetric natural products based on cubic spline interpolation. A piecewise cubic polynomial was constructed using cubic spline interpolation to approximate the boundary curve of the upper half object cross-section based on the boundary points of the object extracted from the image of the object. The polynomial was integrated to obtain the volume of the object. The experimental result reveals that the proposed system achieved an accurate volume measurement result with a mean absolute relative error of 1.03% compared to the water displacement method result.

1. Introduction

Volume measurement has several applications in producing and processing natural products, such as sorting, grading, planting strategy, and plant phenotyping (Siswantoro et al., 2014b; Su et al., 2017; Wang and Li, 2014). Volume and weight can also be used to predict produce density, which plays an important role in determining the chemical composition and detecting defects such as frost damage (Chopin et al., 2017). Measuring the volume of natural products is not a simple task. Generally, a natural product is an irregularly shaped object whose volume cannot be calculated directly using a standard mathematical formula.

The water displacement method based on Archimedes’ principle is an accurate conventional method for measuring volume. However, this method is time-consuming and may be inaccurate for the porous object that can absorb water. Furthermore, it can be considered destructive for some products (Siswantoro et al., 2014b; Wang and Nguang, 2007). A modern approach to measuring the volume of natural products is performed using a computer vision system. This approach is nondestructive and more efficient compared to the water displacement method. Several volume measurement methods have been proposed to measure the volume of natural products by employing either a 3D or 2D computer vision system. The methods extracted some features from the image of the measured object and then used the features to predict volume (Moreda et al., 2009).

In measuring the volume of natural products, the 3D computer vision system required more than one image captured from several views. Generally, the captured images were used to perform 3D object reconstruction. The volume of the measured object was calculated from the reconstructed 3D object either by calculating the number of voxels or using a mathematical formula, as proposed by Chalidabhongse et al. (2006), Lee et al. (2006), Goni et al. (2007), Castillo-Castaneda and Turchiuli (2008), Zhang et al. (2016), Chopin et al. (2017), Concha-Meyer et al. (2018), Jadhav et al. (2019), Li et al. (2021), Mon and ZarAung (2020), and Zavala de Paz et al. (2021). Siswantoro et al. (2014b) have proposed a 3D computer vision system to measure the volume of irregularly shaped food products without performing 3D object reconstruction. The proposed system employed Monte Carlo integration with heuristic adjustment on a 3D bounding box for the product in real-world coordinate. The bounding box was constructed from the captured images using a method proposed by Siswantoro et al. (2013). Even though the volume measurement method using 3D computer vision system could be used to measure the volume of arbitrarily shaped natural product and achieved a good accuracy, the

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method required high computational cost and time.

Wang and Li (2014), Su et al. (2017), Nyalala et al. (2019), and Okinda et al. (2020) have proposed a 3D computer vision system for volume measurement by employing a color and depth camera to capture the images of the measured object. The system proposed by Wang and Li (2014) captured color and depth images from a view only, while that one proposed by Su et al. (2017), Nyalala et al. (2019), and Okinda et al. (2020) required color and depth images from several views. The system proposed by Wang and Li (2014) and Su et al. (2017) constructed a 3D model from color and depth images. Furthermore, the number of voxels in the model and some mathematical formulas were employed to approximate the volume. On the other hand, Nyalala et al. (2019) and Okinda et al. (2020) extracted some 2D and 3D features from the captured image to predict the volume using some regression models.

The 2D computer vision system for volume measurement only requires an image of the measured object captured from a particular view. The captured image is then processed to obtain a silhouette of the object that represents the object cross-section. In general, the 2D computer vision system is used to measure the volume of axi-symmetric objects. A natural product is categorized as an axi-symmetric object if it has a rotation axis, such as egg, lemon, and orange (Siiswantoro et al., 2014a). An axi-symmetric natural product can be considered as a solid of revolution obtained by rotating half of its cross-section around its rotating axis. Therefore, the volume of axi-symmetric natural products can be calculated using a method for calculating the volume of a solid of revolution as long as the equation of the boundary curve of the production cross-section is known (Weir et al., 2010).

Sabliov et al. (2002), Du and Sun (2006), and Wang and Nguang (2007) have proposed methods to measure the volume of axi-symmetric agriculture products from an image by approximating the boundary curve of the product cross-section with a piecewise continuous linear function. With this approach, the volume of the product was obtained by the sum of the right circular conical frustum volume. Huynh et al. (2020) have proposed a real-time volume estimation method for slender axi-symmetric fruits/vegetables by modifying the method proposed by Sabliov et al. (2002) and dividing the cross-section of the measured object into eight segments. The upper and lower segments were assumed to be conical cross-sections, while the rest were conical frustum cross-sections. With this assumption, the volume of the product was obtained by summing the volume of cones and conical frustums.

A slightly different volume approximation method has been proposed by Bridge et al. (2007), Koc (2007), Zhou et al. (2009), Khojastehnazhand et al. (2019), and Widiarsi et al. (2019). They approximated the volume of the axi-symmetric product as the sum of circular disk (thin circular cylinder) volume by assuming the boundary curve of product cross-section is a piecewise constant function. Khojastehnazhand et al. (2009), Khojastehnazhand et al. (2010), and Omid et al. (2010) have proposed volume estimation methods by replacing the circular disk with an elliptical disk. Both disk and conical frustum approaches require a lot of points on the boundary of the object cross-section to obtain good accuracy. It could happen since a linear function or a constant function was employed to represent the boundary curve of the product cross-section, which is generally a nonlinear function. In addition, the method proposed by Sabliov et al. (2002), Bridge et al. (2007), and Koc (2007) were not fully automatic.

The nonlinear approach was also used in the volume measurement of axi-symmetric objects, as proposed by Soltani et al. (2015), Vivek Venkatesh et al. (2015), Ziaratghan et al. (2017), Siiswantoro et al. (2017), Jana et al. (2020), and Nyalala et al. (2021). Soltani et al. (2015) proposed a method to predict volume based on Pappus’ theorem. The volume was obtained by determining the area and centroid of half the object cross-section and employing Pappus’s second centroid theorem. Vivek Venkatesh et al. (2015) treated the boundary of the object cross-section as one of the following shapes: circle, ellipse, or parabolic. The volume was calculated using a formula based on the shape of the boundary. Ziaratghan et al. (2017) and Siiswantoro et al. (2017) used an artificial neural network (ANN) model to predict volume based on 1D and 2D features extracted from the object cross-section. Nyalala et al. (2021) achieved the best prediction for the volume of tomatoes using a support vector regression (SVR) model with a radial basis function (RBF) kernel, based on 1D and 2D features extracted from the object cross-section. A deep neural network (DNN) model was also used to predict the volume of carrots based on five cross-section diameters and the length, as reported by Ornek and Kahramanl Ornek (2021). However, the input features of the DNN model were extracted manually using a vernier caliper and a ruler. Jana et al. (2020) approximated the boundary of object cross-section using 10th order polynomial obtained using interpolation based on some point in the boundary. The polynomial was then integrated to get the volume of the object using an integral for the volume of solid revolution. Although most proposed methods claim to have good accuracy, they are only used to predict the volume of one particular type of object except the method proposed by Vivek Venkatesh et al. (2015).

Image segmentation is an essential step in volume measurement using computer vision. Segmentation aims to localize the object in an image. The accuracy of volume measurement is highly dependent on the result of segmentation. In some previous studies, a common method for image segmentation was automatic thresholding based on the Otsu method (Otsu, 1979). Some morphological operators were also employed after thresholding to improve the segmentation result, as reported by Badaré et al. (2021) and Oliveira et al. (2021).

Siiswantoro and Asmawati (2016) have proposed a new framework for measuring the volume of axi-symmetric natural products based on cubic spline interpolation using a computer vision system. Cubic spline interpolation was used to approximate the boundary curve of object cross-section by constructing a piecewise continuous cubic polynomial. The volume of products was then obtained by integrating the polynomial. Cubic spline interpolation provides a better approximation for a nonlinear smooth function than a piecewise continuous linear function. Furthermore, by employing cubic spline interpolation, the oscillatory nature of high degree polynomial, which usually occurs in ordinary polynomial interpolation, can be avoided (Burden et al., 2009). However, the proposed framework was not implemented to measure the volume of real axi-symmetric natural products. Therefore, the performance of the proposed framework in measuring the volume of real natural products needs to be investigated.

This study aims to propose a rapid and accurate computer vision system for measuring the volume of axi-symmetric natural products based on cubic spline interpolation. The overall process in the proposed system is based on the volume measurement framework proposed by Siiswantoro and Asmawati (2016). Three types of axi-symmetric natural products were used to measure the performance of the proposed system, including eggs, lemons, and oranges. The rest of the paper is organized as follows. Section two describes the materials and methods used in this study. Results and discussion are explained in section three. Finally, conclusions are drawn in section four.

2. Materials and methods

2.1. Natural products samples

An experiment was performed to measure the performance of the proposed computer vision system using three types of axi-symmetric natural products. The samples of natural products used in the experiment were 30 eggs, ten lemons, and ten oranges. All samples were collected randomly from traditional and modern markets in Surabaya, Indonesia. The volume of each product was measured using the proposed system three times, and the average of these three measurements was considered as the approximation volume. For comparison, the volume of each product was also measured using the water displacement method based on Archimedes’ principle to obtain the exact volume.
2.2. Computer vision system

A computer vision system consisting of hardware and software was developed to implement the volume measurement framework proposed by Siswantoro and Asmawati (2016). The hardware used to develop the system was a camera, an illumination source, a computer, and a container box. A Logitech HD Webcam C270h with resolution HD 720p (720 px × 1280 px) was used to acquire the image of the measured object. The camera was connected to a portable computer with a 2.20 GHz Intel Core 2 Duo processor, 2 GB RAM, and Windows 7 operating system using the USB cable. For the illumination source, the system employed two 5 Watt portable LED bulbs connected to the computer using the USB cable to obtain the electricity source. The camera, bulbs, and measured object were contained in a black painted closed container box with dimensions 50 cm × 50 cm × 50 cm to ensure that the system has constant illumination intensity. The arrangement of the hardware and measured object are shown in Fig. 1.

The computer was equipped with software to perform a series of processes for volume measurement, including image acquisition, pre-processing, segmentation, and volume approximation. All processes in the software can be seen in Fig. 2. The software was developed using Visual C++ 2010 with open-source computer vision library OpenCV 231 (Bradski and Kaehler, 2008) and numerical analysis and data processing library ALGLIB 3.10.0 Free Edition (Bochkanov and Bystritsky). A simple and user-friendly user interface was developed to facilitate users who do not have a computer vision background in measuring the volume of axi-symmetric natural produce, as shown in Fig. 3.

2.3. Image acquisition

The computer vision system acquired the image of the measured object using a camera from the top view with a black background. The black background was chosen since the eggs, lemons, and oranges have a different surface color from black. In this condition, the measured object could be easily separated from its background by using image thresholding in the segmentation process. The measured object was located under the camera at about 50 cm.

The image was acquired in RGB (Red Green Blue) color space with a dimension of 640 pixels × 480 pixels and a resolution of 96 dpi both in vertical and horizontal directions. The image was then saved in JPEG format for the following process. In addition, the system could also use an image that has been saved in a JPEG file. The examples of the acquired image are shown in Fig. 4.

2.4. Pre-processing

Pre-processing aims to produce a grayscale image that will be used in segmentation. This step consisted of color transformation and noise reduction. According to Siswantoro et al. (2014b), the segmentation process for the image of natural products could be easily performed in HSV (Hue Saturation Value) color space. Therefore, the acquired image was firstly transformed from RGB color space to HSV color space using a transformation as shown in Eqs. (1)-(3). The example of a transformed image in HSV color space is shown in Fig. 5.

\[
H = \left\{ \begin{array}{ll}
\frac{G - B}{R - \min(R, G, B)} & \text{max}(R, G, B) = R \\
\frac{B - R}{G - \min(R, G, B)} + 2 & \text{max}(R, G, B) = G \\
\frac{R - G}{B - \min(R, G, B)} + 4 & \text{max}(R, G, B) = B \\
0, & \text{max}(R, G, B) \neq 0
\end{array} \right.
\]

\[
S = \max\left(\frac{R, G, B - \min(R, G, B)}{\max(R, G, B)}\right), \quad \text{max}(R, G, B) \neq 0
\]

\[
V = \max(R, G, B)
\]

As can be seen in Fig. 5, the measured object could be easily separated from its background in the S and V channels. Therefore, images in the S and V channels were used to construct a grayscale image Gr. The intensity of every pixel in Gr was obtained from the weighted sum of pixel intensity in the S and V channels, as shown in Eq. (4). The weight of each channel in Eq. (4) was heuristically determined to obtain the optimum segmentation result.

\[
Gr = 0.3S + 0.7V
\]

Finally, a 15 × 15 Gaussian filter (Gonzalez and Woods, 2002) was applied to reduce noise in the grayscale image resulting from the camera. The examples of preprocessing results are shown in Fig. 6.

2.5. Segmentation

Segmentation is a step to separate the object from its background in the grayscale image. This step produced a binary image consisting of white pixels and black pixels. Every pixel in the grayscale image was clustered into a white pixel with binary value 1 for the object and a black pixel with binary value 0 for the background.

The system employed image thresholding to perform segmentation. The threshold value T was automatically determined using the Otsu method (Otsu, 1979). A pixel in the grayscale image with pixel intensity less than T was transformed into a black pixel in the binary image, otherwise to a white pixel. After thresholding, a few object pixels were transformed into the black background and vice versa. Two morphological operators, opening and closing operators with a 5 × 5 ellipse kernel, were used to solve this segmentation problem. The examples of segmentation results can be seen in Fig. 7. From Figs. 4 and 7, it can be seen that the object in the binary image is close to the object in the original image. This fact shows that the Otsu method combined with opening and closing operators is appropriate for the segmentation step in the proposed system.

2.6. Volume approximation

In this step, the volume of the measured object is extracted from the binary image. This step consists of a series of sub-steps, including image cropping, real-world coordinate axes construction, boundary points determination, scale factor determination, cubic spline interpolation, and integration. The detail for every sub-step is explained in the following sub-sections.

2.6.1. Image cropping

Before image cropping, the segmented image was rotated such that the major axis of the object is parallel to the horizontal axis of the image coordinate. This process was used to ensure the object’s rotation axis was parallel to the horizontal axis of the image coordinate. By employing image rotation, the object could be placed in arbitrary
direction during image acquisition.

Image cropping was started by determining an axis-aligned minimum bounding rectangle of the object. The bounding rectangle was determined by finding the minimum and maximum coordinates of white pixels in the binary image both in the horizontal and vertical directions. The binary image was then cropped according to the bounding rectangle. Fig. 8 shows examples of the bounding rectangle and the cropped binary image.

2.6.2. Real-world coordinate axes construction

The system used an integral for the volume of solid revolution to approximate the volume of the measured object. The integral was calculated in a 2D real-world coordinate system. Therefore, the coordinate axes of the 2D real-world coordinate system needed to be constructed. Let \( M \) be the height of the cropped binary image. Two-dimensional real-world coordinate axes were constructed using the following assumptions:

1. The cross-section of the measured object, which is parallel to the rotation axis of the measured object, is located on the \( xy \)-plane.
2. The left-most object pixel is located on the \( y \)-axis.
3. The rotation axis of the measured object is located on \( \lceil \frac{M}{2} \rceil \)th row of the cropped binary image and coincides with the \( x \)-axis, where \( \lceil \frac{M}{2} \rceil \) is the smallest integer greater than or equal to \( M/2 \). Fig. 9 shows the example of constructed real-world coordinate axes.

2.6.3. Boundary points determination

To approximate the boundary curve of the upper half object cross-
section using cubic spline interpolation, a subset of pixels on the boundary of the upper half object cross-section consisting of \( n + 1 \) pixels needed to be determined. The value of \( n \) was chosen depending on the shape of the boundary curve. Since the curvature variation for every type of natural product was different, the value of \( n \) would also be different for every type of natural product.

Fig. 4. The examples of acquired images: (a) egg, (b) lemon, and (c) orange.

Fig. 5. The example of a transformed image in HSV color space: (a) H channel, (b) S channel, and (c) V channel.

Fig. 6. The examples of preprocessing results: (a) egg, (b) lemon, and (c) orange.

Fig. 7. The examples of segmentation results: (a) egg, (b) lemon, and (c) orange.
The experiment was conducted according to the following steps:

1. Choose a random sample from each type of natural product.
2. Capture the image of the sample.
3. Process the image to obtain a cropped binary image B.
4. Choose a value of \( n \) from \( \{2, 3, 4\} \) or \( \{5, 10, 15, 20, 25\} \).
5. Let \( N \) be the width of the cropped binary image, divide the interval \([0, N]\) into \( n \) equal length subintervals with boundary point \( x_i = iN/n \), \( i = 0, 1, \ldots, n \).

6. Determine the coordinate of points on the boundary of the upper half object cross-section at \( x = x_i \) to obtain \( n + 1 \) points \((x_i, y_i), i = 0, 1, \ldots, n \), where

\[
y_i = \begin{cases} 
B(j, 1)/2, & i = 0 \\
\sum_{j=1}^{M} B(j, iN/n)/2, & i = 2, 3, \ldots, n 
\end{cases}.
\]  

(5)

7. Construct a piecewise cubic polynomial using cubic spline interpolation from \((x_i, y_i), i = 0, 1, \ldots, n\) to approximate the boundary curve of the upper half object cross-section.
8. Repeat step 4 until 7 such that an appropriate boundary curve approximation is obtained.

2.6.4. Cubic spline interpolation

Before being used to construct a piecewise cubic polynomial for volume approximation, the coordinates of \( n + 1 \) points on the boundary curve of the upper half of the object cross-section \((x_i, y_i), i = 0, 1, \ldots, n\) were transformed from the image coordinate system into the 2D real-world coordinate system using the following equations.

\[
x_i = kx_i, \quad y_i = ky_i, \quad i = 0, 1, \ldots, n
\]  

(6)

Here, \( k \) is a scale factor used to convert length in the image coordinate system into the 2D real-world coordinate system. The image of a reference object with a known length was captured using the system to obtain the value of \( k \). The value of \( k \) was equal to the ratio between the length of the reference object in the real-world coordinate system and its length in the image coordinate system.

Suppose \( y = f(x), 0 \leq x \leq kN \) is the exact boundary curve of the upper half of the measured object cross-section. A piecewise cubic polynomial \( S(x) \) was then constructed from \((X_i, Y_i^2), i = 0, 1, \ldots, n\), using cubic spline interpolation to approximate \( f(x)^2 \). The polynomial \( S(x) \) was denoted as \( S_j(x) \) on subinterval \([X_j, X_{j+1}]\) for each \( j = 0, 1, 2, \ldots, n - 1 \) as in the following equation.

\[
S_j(x) = a_j + b_j(x - X_j) + c_j(x - X_j)^2 + d_j(x - X_j)^3, \\
\text{for } x \in [X_j, X_{j+1}]
\]  

(7)
The steps used to determine the value of coefficients $a_j, b_j, c_j, d_j$ are provided in Appendix.

2.6.5. Integration

By assuming that a measured object is an axi-symmetric object, then the volume of the measured object can be obtained using the integral for the volume of a solid revolution, as in the following equation (Weir et al., 2010).

$$ V = \pi \int_0^{kN} [f(x)]^2 \, dx $$ (8)

Where $V$ is the volume of the measured object, $y = f(x), 0 \leq x \leq kN$ is the boundary curve of the object cross-section, $k$ is the scale factor, and $N$ is the width of the cropped binary image. Since $[f(x)]^2$ was approximated by $S(x)$, then by using Eq. (7) the integral in Eq. (8) can be expressed as,

$$ V = \pi \sum_{j=0}^{n-1} \int_{X_j}^{X_{j+1}} S(x) \, dx $$

$$ = \pi \sum_{j=0}^{n-1} \left( a_j + b_j (x - X_j) + c_j (x - X_j)^2 + d_j (x - X_j)^3 \right) \left|_{X_j}^{X_{j+1}} \right. $$

$$ = \pi \sum_{j=0}^{n-1} \left( a_j (X_{j+1} - X_j) + \frac{b_j}{2} (X_{j+1} - X_j)^2 + \frac{c_j}{3} (X_{j+1} - X_j)^3 + \frac{d_j}{4} (X_{j+1} - X_j)^4 \right) $$

$$ = \pi \sum_{j=0}^{n-1} \left( a_j \Delta X_j + \frac{b_j}{2} \Delta X_j^2 + \frac{c_j}{3} \Delta X_j^3 + \frac{d_j}{4} \Delta X_j^4 \right) $$ (9)

**Fig. 10.** (a) The acquired image of egg; (b) egg cross section; (c), (e), (g) the results of cubic spline interpolation; (d), (f), (h) the approximation of egg cross section for $n = 2, n = 3, n = 4$, respectively.
where \( \Delta X_j = X_{j+1} - X_j, j = 0, 1, 2, ..., n - 1. \)

2.7. Evaluation

The performance of the proposed system was evaluated using a volume measurement accuracy. The accuracy was measured by comparing the approximation volume measured using the proposed system and the exact volume measured using the water displacement method. The absolute relative error (ARE) was calculated from the approximation volume \( V_A \) and the exact volume \( V_E \) for every product using Eq. (10).

\[
ARE(\%) = \frac{|V_E - V_A|}{V_E} \times 100
\]  

(10)

The linear relationship between the approximation volume and the exact volume was evaluated using the correlation coefficient (\( R \)) and the coefficient of determination (\( R^2 \)). In addition, the paired \( t \)-test was used to examine whether the mean difference between the two measurement results was zero.

Fig. 11. (a) The acquired image of lemon; (b) lemon cross section; (c), (e), (g), (i), (k) the results of cubic spline interpolation; (d), (f), (h), (j), (l) the approximation of lemon cross section for \( n = 5, n = 10, n = 15, n = 20, n = 25 \), respectively.
3. Results and discussion

The preliminary experiment results to determine the number of points on the boundary of the upper half of the object cross-section used for cubic spline interpolation are depicted in Fig. 10, Fig. 11, and Fig. 12. As can be seen in Fig. 10, the approximations of the egg cross-section using cubic spline interpolation were different from the original egg cross-section extracted from the acquired image (Fig. 10 (b)) for $n = 2$ (Fig. 10 (d)) and $n = 3$ (Fig. 10 (f)). However, for $n = 4$ (Fig. 10(h)), the approximation was similar to the original one.

For lemon, cubic spline interpolation needed $n = 25$ (Fig. 11 (l)) to produce an approximation of the lemon cross-section that is similar to the original lemon cross-section. Unlike egg and lemon, cubic spline interpolation only needed $n = 3$ to obtain an appropriate approximation of the orange cross-section. Increasing the value of $n$ did not affect the approximation result. As can be seen in Fig. 12 (f) and (h), there was no difference between the approximation of the orange cross-section with $n = 3$ and $n = 4$. Therefore, the number of points on the boundary of the upper half of the egg, lemon, and orange cross-section used in the experiment were set to 5 (or $n = 4$), 26 (or $n = 25$), and 4 (or $n = 3$), respectively.

The volume measurement result measured using the proposed system and the water displacement method together with its ARE summarized in Table 1. From Table 1, it can be seen that, on average, volume measurement results measured using the proposed system and the water displacement method were close to each other for all samples, which were 115.27 cm$^3$ and 115.23 cm$^3$, respectively. The proposed system produced the mean ARE of 1.03% for all samples, with minimum and maximum ARE being 0.00% and 2.39%, respectively, if compared to the water displacement method. Overall, ARE was less than 2% for 86% of samples. This result shows that the proposed system has high volume measurement accuracy. Furthermore, the standard deviation of ARE was 0.79% for all samples. Therefore, it can be inferred that the proposed system produces high precision volume measurement results. The proposed system had different mean ARE for every type of natural product. The smallest mean ARE was achieved in measuring the volume of eggs (0.94% ± 0.69%), followed by lemons (1.02% ± 0.79%) and oranges (1.30% ± 0.86%). These results occur since the egg had an almost perfect axi-symmetric shape than lemon and orange. In addition, all egg samples had minor variations in shape compared to lemon and orange.

The volume measurement result of the proposed system was highly correlated with the volume measurement results of the water displacement method. For all samples, the correlation coefficient ($R$) of these two volume measurement results was 0.9997. This result shows that the volume measurement result of the proposed system had an excellent linear relationship with the volume measurement results of the water displacement method, as shown in Fig. 13. Since all $R^2$ s were greater than 0.99 (see Fig. 13), it can be concluded that more than 99%
variation of the volume measurement result of the water displacement method can be explained by the volume measurement result proposed system using a linear relationship.

For further analysis, the paired \( t \)-test was used to show no significant difference between the volume measurement result of the proposed system and the water displacement method. The test was performed with a level of significance \( \alpha = 0.05 \) and the following hypothesis,

\[
H_0 : \mu_1 - \mu_2 = 0 \\
H_1 : \mu_1 - \mu_2 \neq 0
\]

where \( \mu_1 \) and \( \mu_2 \) are mean volume measurement results of the proposed system and the water displacement method, respectively. The result of the paired \( t \)-test is tabulated in Table 2.

### Table 1
The summary of volume measurement results measured using the proposed system and the water displacement method.

<table>
<thead>
<tr>
<th>Natural produce</th>
<th>Number of samples</th>
<th>( V_A ) (cm(^3))</th>
<th>( V_E ) (cm(^3))</th>
<th>ARE (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Mean</td>
<td>Min</td>
<td>Max</td>
<td>Std. dev.</td>
</tr>
<tr>
<td>Egg</td>
<td>30</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Lemon</td>
<td>10</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Orange</td>
<td>10</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>All samples</td>
<td>50</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### Table 2
The result of paired \( t \)-test.

<table>
<thead>
<tr>
<th>Paired difference (cm(^3))</th>
<th>Mean (cm(^3))</th>
<th>Std. dev. (cm(^3))</th>
<th>t</th>
<th>d. f.</th>
<th>95% confidence interval for the mean difference</th>
<th>p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Mean</td>
<td>Std. dev.</td>
<td></td>
<td></td>
<td>Lower bound</td>
<td></td>
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<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Upper bound</td>
<td></td>
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As can be seen in Table 2, the mean paired difference between the two-volume measurement results was –0.062 with a 95% confidence interval [–0.6375, 0.5134]. This fact shows that the mean paired difference between the two-volume measurement results was close to zero.
Furthermore, since the p-value of the test was 0.8295 (greater than α), there is insufficient evidence at the level of 0.05 to reject $H_0$. Therefore, it can be concluded that there is no significant difference between the volume measurement result of the proposed system and the water displacement method.

The proposed system is faster than the water displacement method in terms of computational time. The proposed system only required about 0.20 s until 0.25 s in approximating the volume of a sample, while the water displacement method required about 60 s. This required time can be reduced by employing a rapid industrial camera and high-speed computer to acquire and process images. Therefore, there is a possibility to further implement the proposed system into an automated visual inspection system for natural produce grading based on the size in the industry.

For comparison, the volume of all samples was also measured using some existing volume measurement methods based on a single image. All volume measurement results were compared with the volume obtained with the water displacement method by calculating the absolute relative errors. The summaries of the absolute relative errors from all measurement methods are tabulated in Table 3. As shown in Table 3, the proposed system achieved the lowest mean absolute relative error compared to other methods. This result indicates that the proposed system has better accuracy in measuring the volume of axi-symmetric natural products than other methods. In addition, the proposed system also produced the lowest standard deviation of absolute relative error compared to other methods. This result shows that the proposed system is more precise than other methods.

### 4. Conclusions

In this study, a computer vision system was proposed to measure the volume of axi-symmetric natural produces. An image of the measured object was captured from the top view and then processed to obtain a binary image. Some boundary points of the measured object were extracted from the binary image and used to construct a piecewise cubic polynomial using cubic spline interpolation. The polynomial was then used to calculate the volume of the measured object using the integral for the volume of solid of revolution. Fifty samples of axi-symmetric natural products consisting of 30 eggs, ten lemons, and ten oranges were used to validate the proposed system. The experimental results indicate that the proposed system produces a high accuracy volume measurement result with a mean absolute relative error of 1.03% compared to the volume measurement result of the water displacement method. In addition, the statistical analysis result shows that the volume measurement result of the proposed system is not significantly different from the volume measurement result of the water displacement method. For future studies, the application of the proposed system in a visual inspection system for natural product grading based on size needs to be investigated. Furthermore, more samples used to validate the volume measurement model need to be considered to improve the robustness of the model.

### Credit author statement

**Joko Siswantoro**: Conceptualization, Methodology, Software, Investigation, Writing - Review & Editing, Project administration, Funding acquisition. **Endah Asmawati**: Conceptualization, Validation, Formal analysis, Resources. **Muhammad Z. F. N. Siswantoro**: Software, Validation, Investigation, Visualization, Editing, Resources.

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### Appendix

The steps used to determine the value $a_i, b_i, c_i, d_i$ in Eq. (7) are as follows (Burden et al., 2009).

1. For $j = 0, 1, 2, ..., n − 1$ do steps 2 and 3:
   2. Set $a_0 = Y^T_0$.
   3. Set $ΔX_j = X_{j+1} − X_j$.
2. For $j = 1, 2, ..., n − 1$ do step 5:
   5. Set $a_j = \frac{3}{2ΔX_j}(a_{j+1} − a_j) − \frac{3}{ΔX_j}(a_j − a_{j−1})$.
   6. Set $b_j = 0, \mu_j = 0, z_j = 0$.
3. For $j = 1, 2, ..., n − 1$ do steps 8, 9, and 10:
   8. Set $b_j = 2(X_{j+1} − X_j) − ΔX_{j−1}μ_{j−1}$.
   9. Set $μ_j = \frac{ΔX_j}{3}$.
4. Set $c_j = \frac{n − 1}{n} \frac{ΔX_j (a_j + b_j)}{a_j}$.
5. Set $w_j = 0, μ_j = 0, x_j = 0$.
6. For $j = n − 1, n − 2, ..., 0$ do steps 13, 14, and 15:
   13. Set $c_j = z_j − μ_j c_{j+1}$.
   14. Set $d_j = \frac{c_j}{w_j}$. 

### Table 3

<table>
<thead>
<tr>
<th>Authors</th>
<th>Method</th>
<th>ARE (%)</th>
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<tbody>
<tr>
<td></td>
<td>Mean</td>
<td>Std. dev.</td>
</tr>
<tr>
<td>Suhilov et al. (2002),</td>
<td>Conical frustum</td>
<td>1.67</td>
</tr>
<tr>
<td>Du and Sun (2006), Wang</td>
<td>Disks</td>
<td>1.63</td>
</tr>
<tr>
<td>and Nguang (2007)</td>
<td>Pappus’s theorem</td>
<td>1.57</td>
</tr>
<tr>
<td>Bridge et al. (2007),</td>
<td>Sphere, ellipsoid,</td>
<td>10.63</td>
</tr>
<tr>
<td>Koc (2007), Zhou et al.</td>
<td>paraboloid</td>
<td>2.42</td>
</tr>
<tr>
<td>Khajehnejadzand et al.</td>
<td>ANN</td>
<td>1.80</td>
</tr>
<tr>
<td>(2019), Widizari et al.</td>
<td>Cone and conical frustum</td>
<td>3.03</td>
</tr>
<tr>
<td>Soliani et al. (2015)</td>
<td>10th order polynomial interpolation</td>
<td>2.84</td>
</tr>
<tr>
<td>Vivek Venkatesh et al.</td>
<td>RBF SVR</td>
<td>2.17</td>
</tr>
<tr>
<td>et al. (2015)</td>
<td>Cubic spline interpolation</td>
<td>1.03</td>
</tr>
<tr>
<td>Ziaratban et al. (2017)</td>
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<tr>
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<tr>
<td>Huynh et al. (2020)</td>
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<td>Nyalala et al. (2021)</td>
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<tr>
<td>This study</td>
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In this study, a computer vision system was proposed to measure the volume of axi-symmetric natural produce. An image of the measured object was captured from the top view and then processed to obtain a binary image. Some boundary points of the measured object were extracted from the binary image and used to construct a piecewise cubic polynomial using cubic spline interpolation. The polynomial was then used to calculate the volume of the measured object using the integral for the volume of solid of revolution. Fifty samples of axi-symmetric natural produce consisting of 30 eggs, ten lemons, and ten oranges were used to validate the proposed system. The experimental results indicate that the proposed system produces a high accuracy volume measurement result with a mean absolute relative error of 1.03% compared to the volume measurement result of the water displacement method. In addition, the statistical analysis result shows that the volume measurement result of the proposed system is not significantly different from the volume measurement result of the water displacement method. For future studies, the application of the proposed system in a visual inspection system for natural produce grading based on size needs to be investigated. Furthermore, more samples used to validate the volume measurement model need to be considered to improve the robustness of the model.
15. Set $b = \frac{a_1 - a_2}{2\Delta x} - \Delta x \frac{a_1 + a_2}{2}$.
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