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Distributed Model Reference Adaptive Control Based on Cooperative Observer with Optimal Control Modification for Synchronization of Heterogeneous Vehicle Platoon



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https://doi.org/10.18280/mmep.090616 ABSTRACT Received: 29 September 2022 Many distributed controllers for vehicle platoon are designed based on homogeneous assumption and full state information. In reality, vehicle platoon may consist of heterogeneous vehicles and may have limited information due to sensor constraints. Therefore, this paper proposes a distributed model reference adaptive control based on cooperative observer for a heterogeneous vehicle platoon with limited output

cooperative observer design, distributed model reference adaptive control, heterogeneous vehicle platoon, optimal control modification assumption and full state information. In reality, vehicle platoon may consist of heterogeneous vehicles and may have limited information due to sensor constraints. Therefore, this paper proposes a distributed model reference adaptive control based on cooperative observer for a heterogeneous vehicle platoon with limited output information and subjected to uncertain dynamics. Cooperative observer provides a full state estimation of the system. Each follower has a reference model that is designed based on its nominal model and cooperative state variable feedback. Main control system is composed of (i) nominal control that utilized the cooperative state estimation tracking error and (ii) adaptive term that adopted an optimal control modification as an adaptation law. The tracking error of followers to the reference model is shown uniformly bounded and the stability of the platoon is guaranteed through detailed analysis. Performance of the proposed controller is verified by using numerical simulation. To show the advantage of the proposed control, simulation results are compared to the standard distributed model reference adaptive control that is applied for heterogeneous vehicle platoon. It is shown that the proposed control eliminated the high frequency oscillation in the control input.

1. INTRODUCTION

Research on vehicle and transportation technology is progressing rapidly, including electric vehicles [1]. autonomous vehicles [2, 3], connected vehicles [2], traffic management [4] and the possibility of collaboration between unmanned ground vehicles and unmanned aerial vehicles [5]. As we know that the future of transportation is predicted to be connected and automated which allows information to be exchanged between vehicles, pedestrians and infrastructures in the intelligent transportation system (ITS) scheme. With this comprehensive information, various features of cooperative control between vehicles can be embedded in the vehicle for various purposes such as increasing safety, obtaining information about emergency situations, receiving weather reports, creating eco-friendly driving modes and enhancing vehicle mobility. This paper focuses on the aspect of enhancing vehicle mobility with a feature known as a vehicle platoon. Vehicle platoon is a group of vehicles, consisting of 1 leader and N-followers connected via a network of sensors or wireless communication technology, forms a convoy by synchronizing the followers' velocity and acceleration to the leader's state while keeping the desired inter-vehicle distance. Vehicle platoon offers many advantages such as to improve safety and comfort driving, reduce congestion, maximize road capacity, save fuel and reduce air pollution [2]. Therefore, the development of vehicle platoon is a promising breakthrough in the future transportation technology.

Vehicle platoon structure, in multi-agent system (MAS) perspective, is composed of vehicle longitudinal dynamics, information flow topology, spacing policy and distributed controller [6]. In linearized third-order vehicle model [7], vehicle dynamics is depended on its inertial time lag where the value is different from one type vehicle to the others. Vehicle platoon that consists of vehicles with identical inertial time lags is called as a homogeneous vehicle platoon [8]. While, vehicles involved in a heterogeneous vehicle platoon have various inertial time lags [9]. Vehicles exchange information to the other vehicles via inter-vehicle communication technology according to the topology that is used which can either be a directed [10] or undirected topology [11]. There are some common topologies used by researchers for vehicle platoon applications. In directed topologies, four common topologies are used, namely predecessor following (PF) [12], two-predecessor following (TPF) [13], predecessor following leader (PFL) [14], two-predecessor following leader (TPFL) [8]. While, bidirectional (BD) [15] and bidirectional leader (BDL) [8] are common for undirected topologies. To achieve synchronization, a distributed controller is applied to each follower based on specific spacing policy which can either be constant spacing policy (CSP) [16] or constant time heading (CTH) [12].

Since the complexity of real vehicle dynamics, uncertain dynamics is inevitable. The uncertain dynamics can be a result of modeling error [17] or can also be a result of operating condition such as road and vehicle conditions, and environmental factors [9]. Therefore, the uncertain dynamics should be considered in the distributed controller design. A nominal control is a controller that designed based on a nominal model without considering its uncertain dynamics. This controller may decline in performance when the actual vehicle dynamics deviates significantly from its nominal model. In extreme situation, instability of the system may not be avoided [9]. Many literatures have been proposed to handle this issue either for general leader-follower problem or vehicle platoon applications. In order to solve the unknown matched uncertainty and disturbance for general leader-follower MAS, Peng et al. [18] designed a distributed model reference adaptive control. However, leader state is used as a reference model, which will be difficult for followers with no directly communication to the leader. For specific vehicle platoon with CTH and predecessor-following topology, an augmented model reference adaptive control approach was developed by Harfouch et al. [12], while Song et al. [19] designed a set of robust delay feedback controllers. Recently, distributed model reference adaptive control (DMRAC) which has reference model based on its follower's nominal model was proposed by Prayitno et al. [20] for vehicle platoons with CSP and can be applied to various directed and undirected topologies. However, researchers [12, 18, 20] assumed a homogenous system where all platoon vehicles share an identical nominal model.

Homogeneous assumption limits the practicality since in the road, vehicles have different types and manucfaturers [9, 21]. Therefore, a vehicle platoon may consist of passenger cars, buses, vans, trucks and container trucks with variation of brands. This group of vehicles can be categorized as a heterogeneous vehicle platoon. Heavy duty vehicles typically have bigger inertial time lag when compared to passenger vehicles [10]. Since heterogenous vehicles have variation in inertial time lag, each individual vehicle may not perform optimally when the controller is designed based on an identical nominal model that has significant differences from the actual model. Zheng et al. [10] provided controller synthesis and analysis of cooperative control of heterogeneous vehicle platoon for directed acyclic interactions without considering the uncertain dynamics. Applying heterogeneous distributed controller for heterogeneous vehicle platoon subjected to uncertain dynamics is quite challenging. Recently, DMRAC is applied for synchronization of heterogeneous vehicle platoon subjected to uncertain dynamics [22]. However, it still has a problem of high frequency oscillation in the control input. The problem usually happens when fast adaptation is selected [22, 23], which may cause vehicle jerk and energy inefficiency. It is known that large jerk causing less comfort in the driving [24]. However, in certain condition, fast adaptation is required to improve the tracking performance especially when significant uncertainty occurred in the vehicle due to structural damage in the vehicle [25].

Many existing cooperative controllers for general leaderfollower MAS or vehicle platoon are designed based on the assumption that full-state information are available or can be measured [10, 18, 20]. This assumption may make difficulty when full-state information is not available in each follower vehicle. In order to solve this problem, cooperative observer was proposed [26, 27] which utilized neighborhood output estimation error to provide follower's full-state estimation. By utilizing the cooperative state estimation tracking error, a synchronization control to the leader is designed. However, work [26, 27] is designed based on nominal model and applied for homogeneous system.

Consequently, this paper proposes DMRAC based on cooperative observer to achieve synchronization of heterogeneous vehicle platoons subjected to uncertain dynamics. Reference model is designed based on heterogeneous cooperative state variable feedback control (CSVFB). While, main control is composed of a nominal control signal and an adaptive term. In order to solve the problem of high frequency oscillation control input, an optimal control modification (OCM) [28] is adopted as an adaptation law which extended the application for cooperative tracking problem. The main contributions of this paper are:

- (i) Compared to the references [18, 20, 22], the proposed control is designed based on cooperative observer which can be applied for vehicle with limited output information. Compared to the references [10, 26], the proposed control is extended the results to include the uncertain dynamics.
- (ii) Provides the stability analysis of DMARC with OCM which derived based on cooperative tracking problem. DMRAC with OCM eliminates high frequency oscillation in the control input which usually occurred in the standard DMRAC [22] with high adaptation rate.

The rest of the paper presents the problem formulation, details of the proposed controller and main result which will be followed by stability proof. Finally, the performance of the proposed controller is validated through numerical simulations.

2. PROBLEM FORMULATION

Information flow between followers involved in the platoon can be represented by a graph. Denote a graph as $\mathcal{G}(\mathcal{V}, \mathcal{E}, \mathcal{A})$, where $\mathcal{V} = \{v_1, v_2, ..., v_N\}$ is a set of nodes (followers), $\mathcal{E} \subseteq$ $\mathcal{V} \times \mathcal{V}$ is a set of links between the followers and $\mathcal{A} = [a_{ij}] \in$ $\mathbb{R}^{N \times N}$ is an adjacency matrix to represent the information exchange between followers. $a_{ij}=1$ if and only if follower *i* can receive information from follower j, otherwise $a_{ij}=0$. The indegree matrix is defined as $D = diag\{d_{11}, d_{22}, ..., d_{NN}\}$, where $d_{ii} = \sum_{j=1}^{N} a_{ij}$. The Laplacian matrix is represented by $L = [\ell_{ij}] = D - \mathcal{A} \in \mathbb{R}^{N \times N}$ where $\ell_{ii} = d_{ii}$, and the other elements, $\ell_{ij} = -a_{ij}$. A pinning gain matrix is defined as G = $diag\{g_{11}, g_{22}, \dots, g_{NN}\}$, where $g_{ii} = 1$ means that follower *i* receives direct information from the leader, otherwise $g_{ii} = 0$. Let $\tilde{\mathcal{G}}(\tilde{\mathcal{V}}, \tilde{\mathcal{E}})$ be defined such that $\tilde{\mathcal{V}} = \{v_0, v_1, v_2, \dots, v_N\}$ and $\tilde{\mathcal{E}} \subseteq \tilde{\mathcal{V}} \times \tilde{\mathcal{V}}$. Directed graph (digraph) is a graph where all node connections are directed from one node to another node. A topology of vehicle platoon contains a spanning tree if from the leader (as a root node) all followers can be reached by following link arrows.

Assumption 1: $\tilde{\mathcal{G}}$ of vehicle platoon is directed and has at least one spanning tree with the lead vehicle as a root node [29].

Consider a vehicle platoon, where the followers' dynamics can be described as,

$$\dot{x}_i = A_i x_i + B_i \Omega_i u_i + B_i \eta_i(x_i) \tag{1}$$

$$y_i = C_i x_i \tag{2}$$

where, $x_i = [p_i + i \cdot d_r \quad v_i \quad a_i]^T$ is the *i*th follower's state and $y_i \in \mathbb{R}^p$ is the *i*th follower's output. $u_i \in \mathbb{R}^m, \Omega_i, \eta_i(x_i)$ are the control input, control effectiveness, unknown matched uncertainty of the *i*th follower respectively. The uncertainty is parameterized as $\eta_i(x_i) = W_i^T \sigma_i(x_i)$ where $W_i \in \mathbb{R}^{s \times m}$ is an unknown constant weighting matrix and $\sigma_i(x_i) : \mathbb{R}^n \to \mathbb{R}^s$ is a known basis vector function [17].

The leader has a zero input, which can be described as,

$$\dot{x}_0 = A_0 x_0 \tag{3}$$

$$y_0 = C_0 x_0 \tag{4}$$

where, $x_0 = [p_0 \ v_0 \ a_0]^T$ is the leader's state and $y_0 \in \mathbb{R}^p$ is the leader's output. Here, p_i , v_i and a_i for all $i \in \{0,1,..,N\}$ are the position, velocity and acceleration of the *i*th vehicle respectively. While A_i , B_i , and C_i are the system matrix, control matrix, and output matrix of the *i*th vehicle respectively. By defining τ_i as the inertial time lag of the powertrain, A_i and B_i are represented by

$$A_{i} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & -\frac{1}{\tau_{i}} \end{bmatrix}, B_{i} = \begin{bmatrix} 0 \\ 0 \\ \frac{1}{\tau_{i}} \end{bmatrix}, i \in \{0, 1, .., N\}$$
(5)

It is assumed that full state information is not available in each follower. Therefore, a dynamical output regulator in each follower can be designed based on state observers which utilize the available output measurements. Observer provides a full state estimation of the follower, which will be utilized for nominal controller design. Denote the estimation of x_i as \hat{x}_i , while the estimation of y_i as $\hat{y}_i = C_i \hat{x}_i$. The state estimation error is defined as $\tilde{x}_i = x_i - \hat{x}_i$, while the output estimation error is defined as $\tilde{y}_i = y_i - \hat{y}_i$. Inspired by reference [27], let the cooperative output estimation error be defined as,

$$\psi_i = \sum_{j=1}^N a_{ij} \big(\tilde{y}_j - \tilde{y}_i \big) + g_{ii} (\tilde{y}_0 - \tilde{y}_i) \tag{6}$$

The cooperative observer for each follower with uncertain dynamics is designed as,

$$\dot{\hat{x}}_i = A_i \hat{x}_i - c_{1,i} F_i \psi_i + B_i \Omega_i u_i + B_i \eta_i (\hat{x}_i)$$
(7)

where, $c_{1,i} > 0$ and F_i is the observer gain matrix, which can be defined as in reference [27],

$$F_i = P_{1,i} C_i^{\ T} R_i^{-1} \tag{8}$$

where, $P_{1,i}$ is solution of the observer algebraic Riccati equation (ARE)

$$0 = A^T P_{1,i} + P_{1,i}A + Q_i - P_{1,i}C_i^T R_i^{-1}C_i P_{1,r}$$
(9)

where, $Q_i = Q_i^T \in \mathbb{R}^{n \times n} > 0$ and $R_i = R_i^T \in \mathbb{R}^{m \times m} > 0$.

Remark 1: By omitting the uncertain part, the 4th term in Eq. (7), according to the study [27] by choosing $c_{1,i} > 0$ and F_i as in Eq. (8), it is guaranteed that $\tilde{x}_i \to 0$ as $t \to \infty$. While, the remaining uncertain part will be solved by proposing DMRAC with OCM based on the cooperative observer.

Let the reference model for each follower be defined as

$$\dot{x}_{i,r} = A_i x_{i,r} + B_i u_{i,r} \tag{10}$$

where, $x_{i,r} \in \mathbb{R}^n$ is the follower's reference state and $u_{i,r} \in \mathbb{R}^m$ is the reference control signal.

The objective of this paper is to design a distributed controller u_i for each follower in Eq. (1) such that observer, Eq. (7), can track the reference model, Eq. (10), which imply that the followers' output, Eq. (2), synchronize to the leader's output, Eq. (4), with bounded residual error.

3. DMRAC BASED ON COOPERATIVE OBSERVER WITH OCM

The proposed DMRAC based on cooperative observer with OCM is shown in Figure 1, that consists of two main blocks, namely a reference model and a main control system. The reference model generates a reference state $(x_{i,r})$ which will be tracked by the estimated state (\hat{x}_i) . The main control system contains a nominal control signal $(u_{i,n})$ that utilizes the cooperative state estimation error and an adaptive term $(u_{i,a})$ that utilizes the nominal control signal $(u_{i,n})$, the estimated state (\hat{x}_i) , the tracking error to the reference model (e_i) . Nominal control is used to track the leader while adaptive term is used to depress the effect of uncertainty.

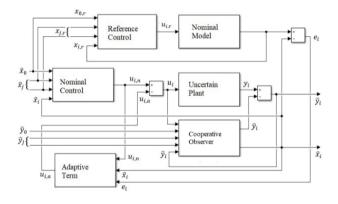


Figure 1. DMRAC based on cooperative observer

3.1 Controller design

The reference control signal is designed as:

$$u_{i,r} = c_{2,i} K_i \left\{ \sum_{j=1}^{N} a_{ij} (x_{j,r} - x_{i,r}) + g_{ii} (x_{0,r} - x_{i,r}) \right\}$$
(11)

where, $c_{2,i}$ is a coupling gain, $K_i \in \mathbb{R}^{m \times n}$ is the feedback gain matrix which defined as:

$$K_i = R_i^{-1} B_i^{T} P_{2,i} . (12)$$

Matrix $P_{2,i}$ is a solution of ARE.

$$0 = A_i^T P_{2,i} + P_{2,i} A_i + Q_i - P_{2,i} B_i R_i^{-1} B_i^T P_{2,i}.$$
 (13)

The control input for each follower, Eq. (1), and cooperative observer, Eq. (7), which composed of a nominal control $(u_{i,n})$ and an adaptive term $(u_{i,a})$, is designed as:

$$u_i = u_{i,n} - u_{i,a}.$$
 (14)

The nominal control input is designed as

$$u_{i,n} = c_{2,i} K_i \hat{\varepsilon}_i \tag{15}$$

with K_i is as given by Eq. (12) and $\hat{\varepsilon}_i$ is cooperative tracking state estimation error that can be represented as:

$$\hat{\varepsilon}_{i} = \sum_{j=1}^{N} a_{ij} (\hat{x}_{j} - \hat{x}_{i}) + g_{ii} (\hat{x}_{0} - \hat{x}_{i}).$$
(16)

By following the procedure [20], the adaptive term is derived as by substituting Eq. (14) into Eq. (7), then adding and subtracting the term $c_{2,i}B_iK_i\hat{\varepsilon}_i$, finally yields:

$$\hat{x}_{i} = A_{i}\hat{x}_{i} + B_{i}u_{i,n} - c_{1,i}F_{i}\psi_{i} + B_{i}\Omega_{i}[\theta_{i}^{T}\Phi_{i}(\sigma_{i}(\hat{x}_{i}), u_{i,n}) - u_{i,a}]$$
(17)

where,

$$\theta_i^T = \begin{bmatrix} \Omega_i^{-1} W_i^T \\ I - \Omega_i^{-1} \end{bmatrix}^T \text{ and } \Phi_i \left(\sigma_i(\hat{x}_i), u_{i,n} \right) = \begin{bmatrix} \sigma_i(\hat{x}_i) \\ u_{i,n} \end{bmatrix}$$
(18)

The adaptive term is constructed as:

$$u_{i,a} = \hat{\theta}_i^T \Phi_i \big(\sigma_i(\hat{x}_i), u_{i,n} \big) \tag{19}$$

where, $\hat{\theta}_i^T$ is the estimated value of θ_i^T . For adaptation law, $\dot{\theta}_i$, an optimal control modification [28] is adopted,

$$\begin{aligned} \hat{\theta}_i \\ &= \gamma_i \Phi_i \big(\sigma_i(\hat{x}_i), u_{i,n}, \psi_i \big) \big[e_i^T P_i \\ &+ \mu_i \Phi_i^T \big(\sigma_i(\hat{x}_i), u_{i,n}, \psi_i \big) \hat{\theta}_i B_i^T P_i A_{i,m}^{-1} \big] B_i \end{aligned}$$
(20)

where, $\gamma_i > 0$ is the adaptation rate, $\mu_i > 0$ is a positive weighting constant, while e_i and $A_{i,m}$ will be defined later.

Remark 2: In order to realize the proposed control, it is assumed that full state information of the reference model is available or can be calculated. The reference states can be treated as virtual state references. All followers exchange information, to connected neighbors, that includes: estimation state (\hat{x}_i) , and output estimation error (\tilde{y}_i) . The reference model uses neighbors' estimation state as neighbors' reference states, i.e. $x_{0,r} = \hat{x}_{0,r}$ and $x_{j,r} = \hat{x}_j$. The leader sends its estimated state (\hat{x}_0) , and output estimation error (\tilde{y}_0) to connected followers. It is assumed that $x_0 = \hat{x}_0$ therefore $\tilde{y}_0 = 0$.

3.2 Tracking error dynamics of followers w.r.t the reference model

Since the observer guarantees $\hat{x}_i \rightarrow x_i$ as $t \rightarrow \infty$ and the fact that $\hat{x}_j = x_{j,r}$, $\hat{x}_0 = x_{0,r}$, therefore for the purpose of stability analysis, the tracking error of each follower w.r.t its reference model can be represented by $e_i = x_i - x_{i,r}$ which resulting the tracking error dynamics,

$$\dot{e}_i = A_{i,m} e_i - B_i \Omega_i \left[\tilde{\theta}_i^T \Phi_i (\sigma_i(x_i), u_{i,n}) \right]$$
(21)

$$A_{i,m} = A_i - c_{2,i}(d_{ii} + g_{ii})B_iK_i.$$
(22)

Here, $\tilde{\theta}_i = \hat{\theta}_i - \theta_i$ is the parameter estimation error and $\sigma_i(x_i) = x_i$ is the known basis function.

3.3 Tracking error dynamics of followers w.r.t the leader

Since the adaptive term suppresed the effects of uncertainties such that $x_i \rightarrow x_{i,r}$ as $t \rightarrow \infty$, therefore, for the purpose of stability analysis, the tracking error w.r.t the leader's state can be expressed by using the reference model as:

$$\rho_i = x_{i,r} - x_{0,r} \tag{23}$$

where, $\rho_i = [\rho_{i,p} \quad \rho_{i,a}]^T$ is the state tracking error to the leader. By following [10], since the leader has zero input which means that the leader moves at constant velocity ($\dot{v}_{0,r} = 0$), the tracking error of follower w.r.t the leader can be defined as:

$$\begin{cases} \rho_{i,p} = p_{i,r} + i \cdot d_r - p_{0,r} \\ \rho_{i,v} = \dot{p}_{i,r} - \dot{p}_{0,r} = v_{i,r} - v_{0,r}. \\ \rho_{i,a} = \ddot{p}_{i,r} - \ddot{p}_{0,r} = a_{i,r} \end{cases}$$
(24)

For the purpose of stability analysis, the control signal in Eq. (11) can be rewritten as:

$$u_{i,r} = c_{2,i} K_i \left[\sum_{j=1}^{N} a_{ij} (\rho_j - \rho_i) - g_{ii} \rho_i \right]$$
(25)

Therefore, the tracking error dynamics of each follower w.r.t the leader is represented as:

$$\begin{cases}
\rho_{i,p} = \rho_{i,v} \\
\dot{\rho}_{i,v} = \rho_{i,a} \\
\dot{\rho}_{i,a} = -\frac{1}{\tau_i}\rho_{i,a} + \frac{1}{\tau_i}c_{2,i}K_i \left[\sum_{j=1}^N a_{ij}(\rho_j - \rho_i) \\
-g_{ii}\rho_i\right]$$
(26)

where, $K_i = [k_{i,p}, k_{i,v}, k_{i,a}]$. The global tracking error dynamics of vehicle platoon, Eq. (26), can be defined as:

$$\dot{\rho} = \hat{A}\rho, \qquad (27)$$

where, $\rho = [\rho_p, \rho_v, \rho_a]^T$ with $\rho_{\pi} = [\rho_{1,\pi}, \rho_{2,\pi}, \dots, \rho_{N,\pi}]^T$ for $\pi \in \{p, v, a\}$. Here,

$$\hat{A} = \begin{bmatrix} 0_N & I_N & 0_N \\ 0_N & 0_N & I_N \\ -\alpha_p H & -\alpha_v H & -\alpha_a H - \vartheta \end{bmatrix},$$
(28)

where, $\alpha_{\pi} = diag(\alpha_{1,\pi}, \alpha_{2,\pi}, ..., \alpha_{N,\pi})$ with $\alpha_{i,\pi} = \frac{1}{\tau_i} c_i k_{i,\pi}$ for $\pi \in \{p, v, a\}, \vartheta = diag(\frac{1}{\tau_1}, \frac{1}{\tau_2}, ..., \frac{1}{\tau_N})$ and H=L+G.

4. MAIN RESULT

Theorem 1. Consider a vehicle platoon with network topology satisfying Assumption 1. Lead vehicle has dynamics

with

as in Eq. (3), followers have dynamics as in Eq. (1) with the observer as in Eq. (7) with observer gain F_i as in Eq. (8) and reference model as in Eq. (10). If each follower applied a distributed controller, Eq. (14), with feedback gain K_i as in Eq. (12) and selecting $c_{2,i}$ such that:

$$c_{2,i} \ge \frac{1}{2(d_{ii} + g_{ii})} \tag{29}$$

along with the adaptation law, Eq. (20), then it will result in stable and uniformly bounded tracking error w.r.t reference model, in compact set C,

$$C = \left\{ \tilde{\theta}_{i}^{T} \Phi_{i}(\sigma_{i}(x_{i}), u_{i,n}) : \left\| \tilde{\theta}_{i}^{T} \Phi_{i}(\sigma_{i}(x_{i}), u_{i,n}) \right\| > \beta \\ = \frac{2\bar{\sigma}(B_{i}^{T} P_{i} A_{i,m}^{-1} B_{i}) \left\| \theta_{i} \Phi_{i}(\sigma_{i}(x_{i}), u_{i,n}) \right\|}{\underline{\sigma}(B_{i}^{T} A_{i,m}^{-T} Q_{i} A_{i,m}^{-1} B_{i})} \right\}$$
(30)

and guarantee the stability of vehicle platoon, Eq. (27). Here, $\underline{\sigma}(\cdot)$ and $\overline{\sigma}(\cdot)$ are the minimum and maximum singular values, respectively.

Proof. For stability proof, it will be shown that the tracking error w.r.t the reference model is uniformly bounded in compact set C, and following by the stability of the closed loop dynamic, Eq. (27).

Proof of the uniformly bounded of e_i.

Lyapunov candidate function is chosen as:

$$V_i(e_i, \tilde{\theta}_i) = e_i^T P_i e_i + \gamma_i^{-1} tr\left(\Omega_i^{\frac{1}{2}} \tilde{\theta}_i^T \tilde{\theta}_i \Omega_i^{\frac{1}{2}}\right).$$
(31)

The first derivative of Eq. (31) along Eq. (21) yields:

$$\dot{V}_{i} = e_{i}^{T} \left[P_{i} A_{i,m} + A_{i,m}^{T} P_{i} \right] e_{i} - 2e_{i}^{T} P_{i} B_{i} \Omega_{i} \tilde{\theta}_{i}^{T} \Phi_{i} \left(\sigma_{i}(x_{i}), u_{i,n} \right) + 2\gamma^{-1} tr \left(\Omega_{i} \tilde{\theta}_{i}^{T} \dot{\theta}_{i} \right)$$

$$(32)$$

Substituting Eq. (20) and re-arranging yields:

$$\dot{V}_{i} = e_{i}^{T} [P_{i}A_{i,m} + A_{i,m}^{T}P_{i}]e_{i} - 2e_{i}^{T}P_{i}B_{i}\Omega_{i}\tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n}) + 2tr(\Omega_{i}\tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n})\{e_{i}^{T}P_{i}B_{i} + \mu_{i}\Phi_{i}^{T}(\sigma_{i}(x_{i}), u_{i,n})\hat{\theta}_{i}B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i}\})$$
(33)

Using trace identity $tr(a^Tb) = ba^T$, Eq. (33) can be reexpressed as:

$$\dot{V}_{i} = e_{i}^{T} [P_{i}A_{i,m} + A_{i,m}^{T}P_{i}]e_{i} - 2e_{i}^{T}P_{i}B_{i}\Omega_{i}\tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n}) + 2\{e_{i}^{T}P_{i}B_{i} + \mu_{i}\Phi_{i}^{T}(\sigma_{i}(x_{i}), u_{i,n})\hat{\theta}_{i}B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i}\} \qquad (34)$$

$$\Omega_{i}\tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n})$$

After some elimination, finally, it obtained that:

$$\dot{V}_{i} = e_{i}^{T} [P_{i}A_{i,m} + A_{i,m}^{T}P_{i}]e_{i} + 2\mu_{i}\Omega_{i}\Phi_{i}^{T}(\sigma_{i}(x_{i}), u_{i,n})\hat{\theta}_{i}B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i} \qquad (35)$$
$$\tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n})$$

It is known that $\theta_i + \tilde{\theta}_i = \hat{\theta}_i$, therefore Eq. (35) become:

$$\dot{V}_{i} = e_{i}^{T} [P_{i}A_{i,m} + A_{i,m}^{T}P_{i}]e_{i} + 2\mu_{i}\Omega_{i}\phi_{i}^{T}(\sigma_{i}(x_{i}), u_{i,n})\theta_{i}B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i} \\ \tilde{\theta}_{i}^{T}\phi_{i}(\sigma_{i}(x_{i}), u_{i,n}) + 2\mu_{i}\Omega_{i}\phi_{i}^{T}(\sigma_{i}(x_{i}), u_{i,n})\tilde{\theta}_{i} \\ B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i}\tilde{\theta}_{i}^{T}\phi_{i}(\sigma_{i}(x_{i}), u_{i,n})$$
(36)

Consider the first term in Eq. (36), by substituting Eq. (22), $P_i A_{i,m} + A_{i,m}^T P_i$ becomes:

$$P_{i}A_{i,m} + A_{i,m}{}^{T}P_{i} = -Q_{i} - (2c_{2,i}(d_{ii} + g_{ii}) - 1)K_{i}{}^{T}R_{i}K_{i}$$
(37)

Therefore, Eq. (36) becomes:

$$\dot{V}_{i} = e_{i}^{T} \left[-Q_{i} - (2c_{2,i}(d_{ii} + g_{ii}) - 1)K_{i}^{T}R_{i}K_{i} \right] e_{i}
+ 2\mu_{i}\Omega_{i}\phi_{i}^{T} \left(\sigma_{i}(x_{i}), u_{i,n}\right) \theta_{i}B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i}
\tilde{\theta}_{i}^{T}\phi_{i} \left(\sigma_{i}(x_{i}), u_{i,n}\right) + 2\mu_{i}\Omega_{i}\phi_{i}^{T} \left(\sigma_{i}(x_{i}), u_{i,n}\right) \tilde{\theta}_{i}
B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i}\tilde{\theta}_{i}^{T}\phi_{i} \left(\sigma_{i}(x_{i}), u_{i,n}\right)$$
(38)

Following [28, 30], it can be seen that the sign-definiteness of Eq. (38) is rely on the sign-definiteness of $P_i A_{i,m}^{-1}$. Where, the evaluation of sign-definiteness of $P_i A_{i,m}^{-1}$ can be conducted by using the negative definite matrix property, i.e. "A general real matrix M is negative definite if and only if its symmetric part $M_s = \frac{1}{2}(M + M^T)$ is also negative definite". Denote $M = P_i A_{i,m}^{-1}$, then Eq. (37) can be pre and post multiplied by $\frac{1}{2}A_{i,m}^{-T}$ and $A_{i,m}^{-1}$, finally yields:

$$\frac{\frac{1}{2}(P_{i}A_{i,m}^{-1} + A_{i,m}^{-T}P_{i})}{= -\frac{1}{2}[A_{i,m}^{-T}Q_{i}A_{i,m}^{-1} + A_{i,m}^{-T}(2c_{2,i}(d_{i} + g_{i}) - 1)K_{i}^{T}R_{i}K_{i}A_{i,m}^{-1}]}$$
(39)

By selecting a coupling gain $c_{2,i}$ that satisfies Eq. (29), the right-hand side of Eq. (39) is negative definite which mean that $M = P_i A_{i,m}^{-1} < 0$. This matrix can be decomposed into the sum of a symmetric matrix M_s and an anti-symmetric matrix N, i.e. $M = M_s + N$, where $M_s = \frac{1}{2} (P_i A_{i,m}^{-1} + A_{i,m}^{-T} P_i)$ and $N = \frac{1}{2} (P_i A_{i,m}^{-1} - A_{i,m}^{-T} P_i)$. By choosing y as a vector of matching dimensions, then pre and post multiplied $M = M_s + N$ by y^T and y, considering that N is anti-symmetric matrix such that $y^T Ny = 0$, finally yields:

$$y^{T} P_{i} A_{i,m}^{-1} y = -\frac{1}{2} y^{T} [A_{i,m}^{-T} Q_{i} A_{i,m}^{-1} + A_{i,m}^{-T} (2c_{2,i} (d_{ii} + g_{ii}) - 1) K_{i}^{T} R_{i} K_{i} A_{i,m}^{-1}] y$$

$$(40)$$

Let choose $y = B_i \tilde{\theta}_i^T \Phi_i (\sigma_i(x_i), u_{i,n})$, then Eq. (38) can be represented as:

$$V_{i} = e_{i}^{T} \left[-Q_{i} - (2c_{2,i}(d_{ii} + g_{ii}) - 1)K_{i}^{T}R_{i}K_{i} \right] e_{i} + 2\mu_{i}\Omega_{i}\Phi_{i}^{T} \left(\sigma_{i}(x_{i}), u_{i,n}\right) \theta_{i}B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i}$$

$$\tilde{\theta}_{i}^{T}\Phi_{i} \left(\sigma_{i}(x_{i}), u_{i,n}\right) - \mu_{i}\Omega_{i}\Phi_{i}^{T} \left(\sigma_{i}(x_{i}), u_{i,n}\right) \tilde{\theta}_{i}B_{i}^{T}$$
(41)

$$\begin{bmatrix} A_{i,m}^{-T}Q_{i}A_{i,m}^{-1} + A_{i,m}^{-T}(2c_{2,i}(d_{ii} + g_{ii})) \\ -1)K_{i}^{T}R_{i}K_{i}A_{i,m}^{-1} \end{bmatrix} B_{i}\tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n})$$

By choosing a coupling gain $c_{2,i}$ that satisfies Eq. (29), the upper bound of \dot{V}_i is:

$$\begin{split} \dot{V}_{i} &\leq -\underline{\sigma}(Q_{i}) \|e_{i}\|^{2} - \mu_{i}\Omega_{i}\underline{\sigma}(B_{i}^{T}A_{i,m}^{-T}Q_{i}A_{i,m}^{-1}B_{i}) \\ & \left\|\tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n})\right\|^{2} \\ + 2\mu_{i}\Omega_{i}\overline{\sigma}(B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i}) \|\theta_{i}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n})\| \\ & \left\|\tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n})\right\| \end{split}$$
(42)

Thus, with:

$$\frac{\left\|\tilde{\theta}_{i}^{T} \Phi_{i}\left(\sigma_{i}(x_{i}), u_{i,n}\right)\right\| \geq}{2\bar{\sigma}\left(B_{i}^{T} P_{i} A_{i,m}^{-1} B_{i}\right)\left\|\theta_{i} \Phi_{i}\left(\sigma_{i}(x_{i}), u_{i,n}\right)\right\|}{\underline{\sigma}\left(B_{i}^{T} A_{i,m}^{-T} Q_{i} A_{i,m}^{-1} B_{i}\right)}$$

$$(43)$$

render $\dot{V}_i \leq 0$. Since,

$$V_{i}(t \to \infty) \leq V_{i}(0) - \underline{\sigma}(Q_{i}) \int_{0}^{\infty} ||e_{i}||^{2} dt - \mu_{i}\Omega_{i}\underline{\sigma}(B_{i}^{T}A_{i,m}^{-T}Q_{i}A_{i,m}^{-1}B_{i}) \\ \int_{0}^{\infty} \left\| \tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n}) \right\|^{2} dt + 2\mu_{i}\Omega_{i}\overline{\sigma}(B_{i}^{T}P_{i}A_{i,m}^{-1}B_{i})$$

$$2\mu_{i}\Omega_{i}\overline{\sigma}(B_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n})) \left\| \tilde{\theta}_{i}^{T}\Phi_{i}(\sigma_{i}(x_{i}), u_{i,n}) \right\| dt < \infty$$

$$(44)$$

It means that $V_i(t \to \infty) < V_i(0)$, therefore V_i decrease inside a compact set $C \subset \mathbb{R}^n$ as described in Eq. (30). However, V_i increase inside the complementary set $C = \{\|\tilde{\theta}_i^T \Phi_i(\sigma_i(x_i), u_{i,n})\| \in \mathbb{R}^n: \|\tilde{\theta}_i^T \Phi_i(\sigma_i(x_i), u_{i,n})\| \le \beta\}$ which contain $\tilde{\theta}_i^T = 0$ and will inside C. By the LaSalle's extension of the Lyapunov method, $\tilde{\theta}_i$ is uniformly bounded. It implies that the tracking error e_i is uniformly bounded.

Proof of the stability of p.

Inspired by reference [10], stability analysis of the platoon can be conducted by using the characteristic equation of Eq. (27) as:

$$\left|\lambda I_N - \hat{A}\right| = \begin{vmatrix}\lambda I_N & -I_N & 0_N\\ 0_N & \lambda I_N & -I_N\\ \alpha_p H & \alpha_v H & \lambda I_N + \alpha_a H + \vartheta\end{vmatrix}$$
(45)

$$= \lambda^3 I_N + \lambda^2 (\alpha_a H + \vartheta) + \lambda \alpha_v H + \alpha_p H$$
(46)

Here, α_p , α_v , α_a , ϑ are diagonal matrices and *H* is lower triangular matrix, therefore Eq. (46) can be described as:

$$\begin{aligned} |\lambda I_N - \hat{A}| &= \prod_{i=1}^N \lambda^3 + \lambda^2 \left[\alpha_{i,a} (d_{ii} + g_{ii}) + \frac{1}{\tau_i} \right] \\ &+ \lambda [\alpha_{i,\nu} (d_{ii} + g_{ii})] + \alpha_{i,p} (d_{ii} + g_{ii}) \end{aligned}$$
(47)

The stability of the global tracking error dynamics Eq. (27) is equivalent to the stability of the following *N* characteristic equations,

$$\lambda^{3} + \lambda^{2} \left[\alpha_{i,a}(d_{ii} + g_{ii}) + \frac{1}{\tau_{i}} \right] + \lambda \left[\alpha_{i,\nu}(d_{ii} + g_{ii}) \right] + \alpha_{i,\nu}(d_{ii} + g_{ii}) = 0, \ i = 1, 2, ..., N$$
(48)

Since *H* is lower triangular matrix, it is seen that \hat{A} in Eq. (28) is composed of $A_i - c_{2,i}(d_{ii} + g_{ii})B_iK_i$ which is equal to $A_{i,m}$ as in Eq. (22). From Eq. (37), by choosing the proper $c_{2,i}$ it shown that $A_{i,m}$ is Hurwitz for all *i*. Therefore, all the eigenvalues of Eq. (48) have negative real parts and guarantee stability of vehicle platoon.

This completes the proof.

5. NUMERICAL SIMULATION

For numerical simulation analysis, a heterogeneous vehicle platoon consisted of 1-leader and 5-followers, formed based on PF topology and constant spacing policy with the desired inter-vehicular distance $d_r = 5$ m, is used, Figure 2.

Vehicles have nominal inertial time lags $\tau_0 = 0.6$, $\tau_1 = 0.25$, $\tau_2 = 0.27$, $\tau_3 = 0.3$, $\tau_4 = 0.5$ and $\tau_5 = 0.7$. Followers are subjected to uncertainty in the inertial time lag which represented by following constant weighting matrices: $W_1^T = [0 \ 0 \ 0.286]$, $W_2^T = [0 \ 0 \ 0.27]$, $W_3^T = [0 \ 0 \ 0.926]$, $W_4^T = [0 \ 0 \ 0.286]$ and $W_5^T = [0 \ 0 \ 0.125]$. The actual control effectiveness for followers is $\Omega_1 = 0.5$, $\Omega_2 = 0.6$, $\Omega_3 = 0.6$, $\Omega_4 = 0.7$ and $\Omega_5 = 0.7$. It is assumed that only position and velocity information can be obtained, therefore the output matrix is,

$$C_i = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \tag{49}$$

The initial states of vehicles are as follows: $x_0(0) = [60,20,0]^T$, $x_1(0) = [40,18,0]^T$, $x_2(0) = [25,19,0]^T$, $x_3(0) = [17,22,0]^T$, $x_4(0) = [10,21,0]^T$ and $x_5(0) = [0,17,0]^T$, while the initial state of the estimated state are selected near the initial states, namely $\hat{x}_1(0) = [38,17,0]^T$, $\hat{x}_2(0) = [27,18,0]^T$, $\hat{x}_3(0) = [16,23,0]^T$, $\hat{x}_4(0) = [12,22,0]^T$ and $\hat{x}_5(0) = [2,16,0]^T$.

The coupling gains for the observer and nominal controls, the adaptation rates and the weighting constant are selected to be the same for each follower, namely $c_{1,i} = 0.1$ and $c_{2,i} = 0.5$, $\gamma_i = 1$ and $\mu_i = 0.2$ respectively. While the observer gain, F_i , and the feedback gain, K_i are obtained according to Eq. (8) and Eq. (12) respectively by selecting $Q_i = I_{3\times 3}$ and $R_i = 0.1$.

Remark 3: In practice, the control parameters that require tuning are Q_i , R_i , $c_{1,i}$, $c_{2,i}$, γ_i and μ_i . It should be noted that the choice of Q_i , R_i , $c_{1,i}$ and $c_{2,i}$, values is a trade-off between consensus tracking performance and a reasonable control signal. The larger the value of Q_i , $c_{1,i}$ and $c_{2,i}$, the better the consensus tracking performance, conversely, the smaller the value of R_i , the better the consensus tracking performance. However, the increase in performance will be followed by an increase in the control signal [22]. The higher the adaptation rate, γ_i , the faster the follower can track to reference model, but it is followed by the possibility of high-frequency oscillations of the control signal [23]. The greater the value of μ_i , the greater the frequency attenuation of the control signal.

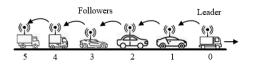


Figure 2. A vehicle platoon with PF topology [22]

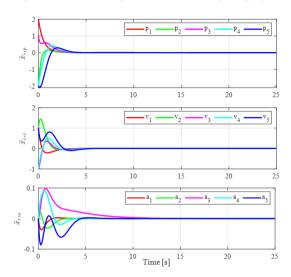


Figure 3. The state estimation error, \hat{x}_i

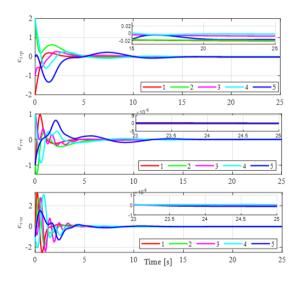


Figure 4. Tracking error with respect of reference model, e_i

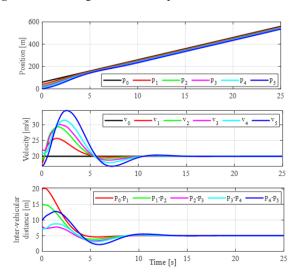


Figure 5. Synchronization of the platoon

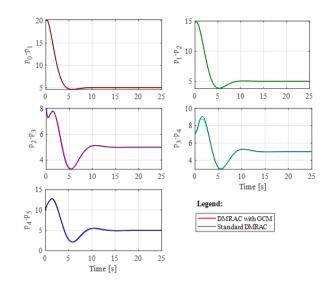


Figure 6. Inter-vehicular distance comparison between the proposed DMRAC with OCM and the standard DMRAC

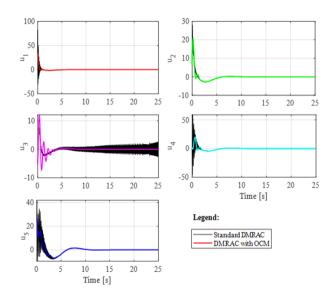


Figure 7. Control input comparison between proposed DMRAC and standard DMRAC

Table 1. Tracking error w.r.t the reference model

Tracking error (t≥20s)	Min	Max
Distance [m]	-0.026	0.006
Velocity [m/s]	-0.0003	-0.0001
Acceleration [m/s ²]	-0.00007	-0.00004

Numerical simulations show that the state estimation error is approach zero as time approach infinity, Figure 3. While, in Figure 4, it is shown that the tracking error of followers w.r.t the reference model is bounded in some constant values, Table 1. Stability and synchronization of the heterogeneous vehicle platoon is shown in Figure 5. It is seen that followers able to keep the inter-vehicular distance as required, with small bounded residual error, namely ± 0.025 m.

For further analysis, the results were compared with the standard DMRAC [22] which was modified to be designed based on the cooperative observer and applied to heterogeneous vehicle platoons (standard DMRAC). Here, the inter-vehicular distance for both schemes is analyzed for each follower as shown in Figure 6. It can be seen that the

performance of the proposed controller is relatively the same with standard DMRAC, however the proposed controller able to eliminate high frequency oscillation in the control input which occurred in the standard DMRAC, Figure 7. This control signal improvements have implications for significant improvements in vehicle jerks and driving comfort, since the control input represents the desired acceleration of the vehicle. Moreover, with smooth trajectory control input, it will improve energy efficiency.

6. CONCLUSIONS

This paper presented a distributed model reference adaptive control based on cooperative observer for synchronization of heterogeneous vehicle platoon. The control scheme utilized a reference model and a main control system. The reference model generated a reference state that will be tracked by the estimated state which provided by the cooperative observer. The main control system consisted of two terms, namely (i) a nominal control that utilized the cooperative state estimation error and (ii) an adaptive term that adopted optimal control modification. Through stability analysis and numerical simulation, it is shown that the state estimation error approach zero as time approach infinity. Moreover, it shown that the tracking error w.r.t the reference state is bounded in some small constant values which implied that the follower synchronized the leader state with small residual error. The proposed control exhibited the advantage of eliminating high frequency oscillation in the control input which usually occurred in the standard DMRAC with high adaptation rate. This paper still assumes that the leader moves at constant velocity and communication between vehicles is in ideal conditions. Therefore, future works may focus on several implementation issues such as explicitly considering poor communication problems in controller design and stability analysis and on the case that lead vehicle has possibility to move at time-varying velocity.

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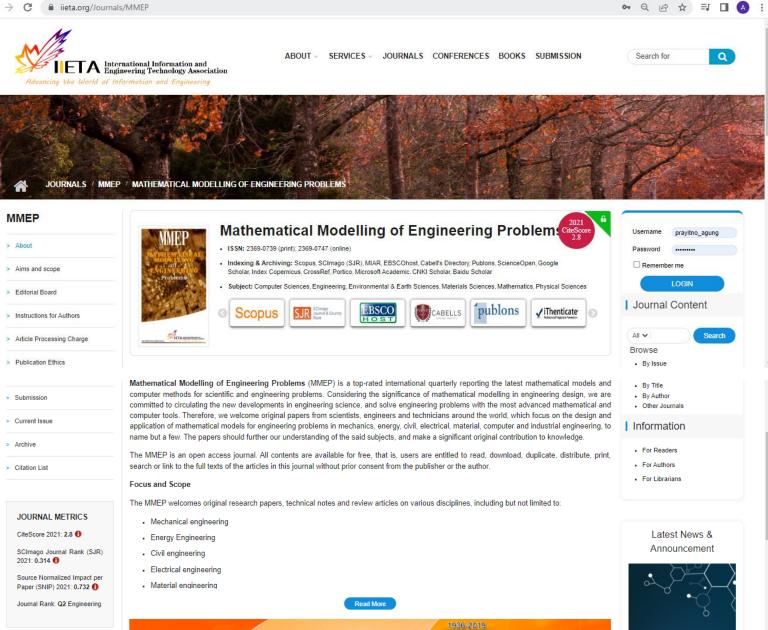
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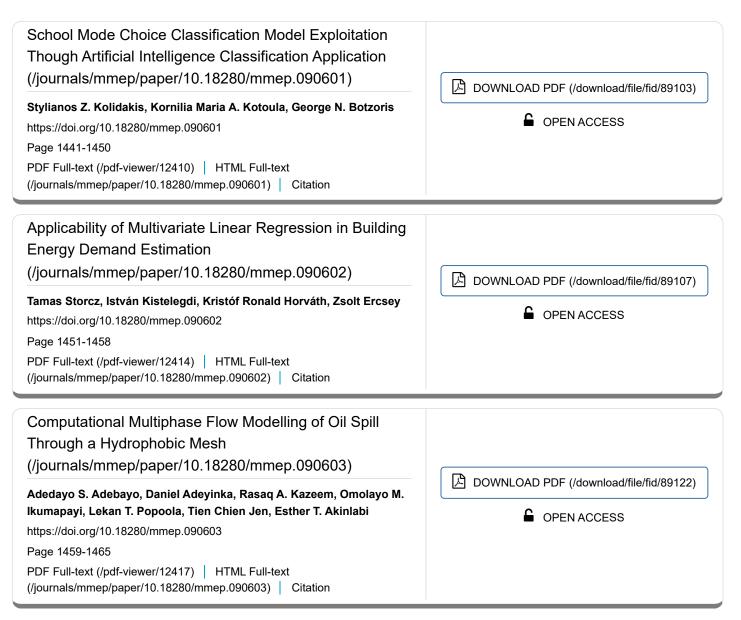
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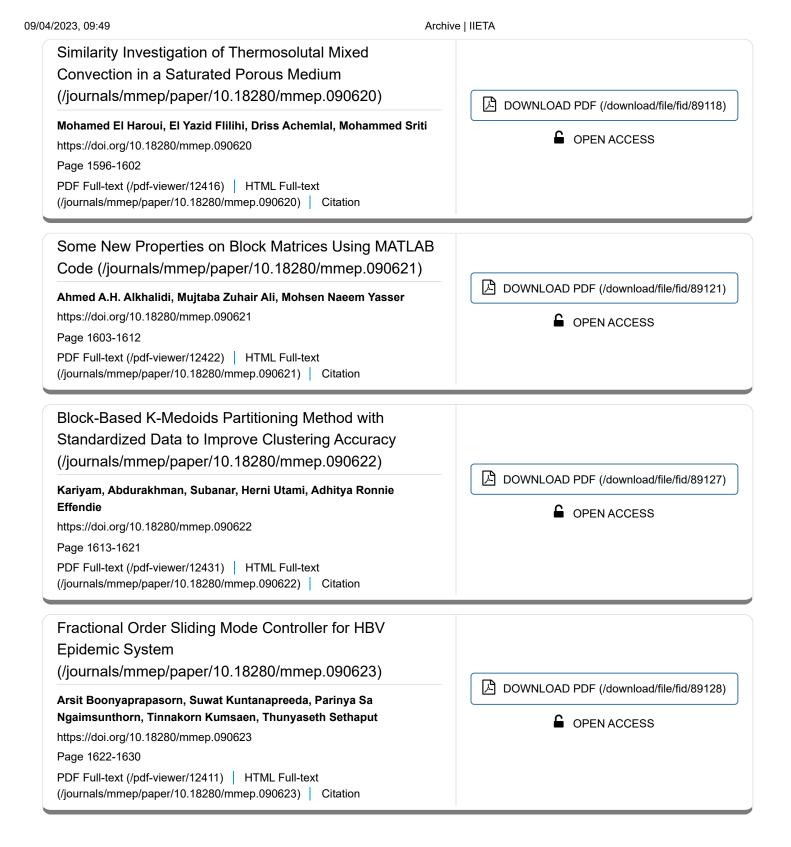
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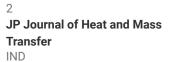
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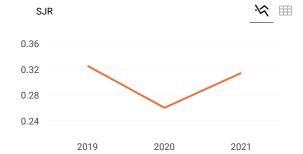
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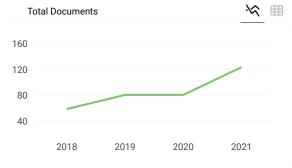
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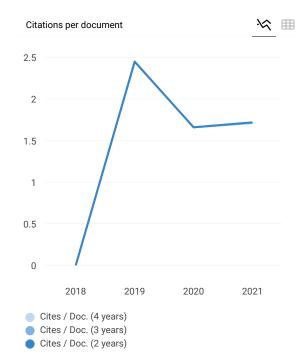
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